

16/4/2020

(3)

Date: \_\_\_\_\_

Page: \_\_\_\_\_



M. 5

The 4 - Every odd integer is of the form

(i)  $2q+1$  (ii)  $2q-1$  (iii)  $4q+1$  (iv)  $\pm(4q+1)$

Proof -

We know that  $2q$  is an even integer, so we have  $2q+1$  and  $2q-1$  are odd integers. Also we know that every integer has one of the form  $4q$ ,  $(4q+1)$ ,  $(4q+2)$  in which  $4q$ ,  $4q+2$  are even integers. Thus  $(4q+1)$  are odd integers. Now  $4q-1 = -(-4q+1) = -1(-q+1)$ . So  $\pm(4q+1)$  is an odd integer.

M. 6

The 5 Do yourself.

M. 7

The 6 one of every three consecutive integers is divisible by 3.

Proof - Let  $a, (a+1), (a+2)$  be any three consecutive integers. Then  $a$  is of the form  $3q, (3q+1)$  or  $(3q-1)$ . If  $a = 3q$  then it is divisible by 3. If  $a = 3q+1$  then  $a+2 = 3q+1+2 = 3q+3 = 3(q+1)$ , means divisible by 3. If  $a = 3q-1$  then  $a+1 = 3q-1+1 = 3q$ , divisible by 3. Thus one of every three consecutive integers is divisible by 3.

The 7 - Do yourself.

Date: \_\_\_\_\_

Page: \_\_\_\_\_

Ex :- find the minimal remainder of 217 with respect to 39.

Ans :-

we have

$$217 = 39 \times 5 + 22$$

$$\boxed{a = bq + r} \quad r > \frac{b}{2}$$

$$a = 217, \quad b = 39, \quad r = 22$$

$$\text{Here remainder } r = 22 > \frac{39}{2}$$

Now the minimal remainder is

$$= -(39 - 22) = -17$$

$$\boxed{-(b - r) = \text{minimal remainder}}$$

This is verified as -

$$217 = 39 \times 6 - 1(17)$$

where

$$0 < 17 < \frac{39}{2}$$